## NWERC 2021 presentation of practice solutions

November 20, 2021

Problem Author: Nils Gustafsson

## Problem

Given $n$ pairs of (time, location), find the smallest length of a cloud that, moving at a speed of at most $1 \mathrm{~m} / \mathrm{s}$, can cover all the locations at the corresponding times.

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- Binary search over the length of the cloud. Complexity: $\mathcal{O}(n \log n)$.

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Statistics: 152 submissions, 43 accepted, 49 unknown

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- Let $a$ be the side length of the hexagon.
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- The hexagon is made up of six equilateral triangles, so the area is $A=6 \cdot \frac{\sqrt{3}}{4} a^{2}$.

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- Combine the equations and solve for the perimeter:

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p=6 \cdot \sqrt{\frac{4 A}{6 \sqrt{3}}}
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## B: Basalt Breakdown

Problem Author: Paul Wild

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Given the area of a regular hexagon, find its perimeter.

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- The perimeter is $p=6 a$.
- The hexagon is made up of six equilateral triangles, so the area is $A=6 \cdot \frac{\sqrt{3}}{4} a^{2}$.
- Combine the equations and solve for the perimeter:

$$
p=6 \cdot \sqrt{\frac{4 A}{6 \sqrt{3}}}
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Statistics: 141 submissions, 100 accepted, 9 unknown

## Alternative Solution

## Google

## perimeter of regular hexagon in terms of area

Q All
© Images
国 News

- Videos
$\bigcirc$ Maps
: More

About 437.000 results ( 0,44 seconds)

Regular hexagon
Solve for perimeter -

$$
P=3^{1 / 4} \sqrt{8 A}
$$ - - -

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- Compare one of the coins in the pair (say a) to any other coin. If they have different weight, then $a$ is the odd one out. If they have equal weight, then $b$ is the odd one out.


## C: Counterfeit Coin

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Given $n-1$ coins of the same weight and one of a different weight, find the coin of different weight by weighing at most $\left\lceil\frac{n}{2}\right\rceil$ times.

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- Compare one of the coins in the pair (say a) to any other coin. If they have different weight, then $a$ is the odd one out. If they have equal weight, then $b$ is the odd one out.

Statistics: 239 submissions, 81 accepted, 34 unknown

## Language stats



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- Time Limit Exceeded means your submission took too much time;
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- For Kotlin, make a fun main function, use the .ks extension, and for e.g. file.ks use FileKs as the mainclass.


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- You can not hide the IDE widget on the problem web pages.

